

Mark Scheme (Results)

Summer 2015

Pearson Edexcel International A Level in Statistics 1 (WST01/01)

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### General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

#### PEARSON EDEXCEL GCE MATHEMATICS

## **General Instructions for Marking**

- 1. The total number of marks for the paper is 75
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- M marks: Method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.

### 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod benefit of doubt
- ft follow through
- the symbol  $\sqrt{}$  will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- d... or dep dependent
- indep independent
- dp decimal places
- sf significant figures
- \* The answer is printed on the paper or ag- answer given
- L or d... The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. If a candidate makes more than one attempt at any question:
  - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
  - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer.

# June 2015 WST01 STATISTICS 1 Mark Scheme

Question	Scheme			
1. (a)	F(4) = 1			
	$4^2 k = 1 \Rightarrow k = \frac{1}{16}$			
(b)	e.g. $P(X = 2) = F(2) - F(1) = \frac{4}{16} - \frac{1}{16} = \frac{3}{16}$			
	[x] 1 2 3 4			
	1 2 5 7			
	(0.0625) (0.1875) (0.3125) (0.4375)	A1		
		(2) <b>Total 4</b>		
(a)	Notes  M1 for writing or using F(4)=1			
(a)	1			
	A1 for $\frac{1}{16}$ or 0.0625 (Answer only scores 2 out of 2)			
(b)	M1 for correct use of $F(x)$ to find $P(X = 2, 3, \text{ or } 4)$ (can follow through their $k$ , $3k$ , $5k$ , $7k$ ). May be implied by at least two correct probabilities or correct follow through.			
	A1 for a fully correct probability distribution. Allow exact decimals. Ignore incorrect or missing labels if table is all correct.			

Question	Scheme		Marks
2. (a)	$S_{xy} = 1474.1 - \frac{441.5 \times 59.8}{20} = 154.015$	awrt <u><b>154</b></u>	M1A1
	$S_{xx} = 11261.25 - \frac{441.5^2}{20} = 1515.1375$	awrt <u>1520</u>	A1
(J.)	F		(3)
(D)	$b = \left[\frac{S_{xy}}{S_{xx}}\right] = \frac{"154.015"}{"1515.1375"} = \left[0.10165084\right]$ $[a = \overline{y} - b\overline{x} \rightarrow]  a = \frac{59.8}{20} - b' \times \frac{441.5}{20} = \left[0.7460577\right]$ $y = 0.746 + 0.102x$		M1
	$[a = \overline{y} - b\overline{x} \rightarrow]$ $a = \frac{59.8}{20} - b' \times \frac{441.5}{20} = [0.7460577]$		M1
	y = 0.746 + 0.102x		A1
			(3)
(c)	$\frac{v}{100000} = 0.746' + 0.102' \left(\frac{s - 50}{10}\right)$		M1
	v = 23780.34997 + 1016.508403s	c = awrt  23600-23800	A1
		$d = \operatorname{awrt} \overline{1020^{**}}$	A1
(d)	$v = 23780.34997 + 1016.508403 \times 130 = 155926.44236$	awrt <b>156000</b>	(3) M1A1
. ,			(2)
(e)	For each (additional) $\underline{1 \text{ m}^2}$ in floor size, the value of the '£1020'	house increases by	B1 (1)
<b>(f)</b>	[31 <i>d</i> =] £31511.76	awrt (£) <u><b>32000</b></u>	B1 (1)
			(1) <b>Total 13</b>
	Notes		1044110
(a)	M1 for one correct expression for $S_{xy}$ or $S_{xx}$		
	1 <sup>st</sup> A1 for either $S_{xy}$ = awrt 154 or $S_{xx}$ = awrt 1520		
(b)	2 <sup>nd</sup> A1 for both		
(b)	1 <sup>st</sup> M1 for a correct expression for $b$ (ft their $S_{xy} \neq 1474.1$ ) 2 <sup>nd</sup> M1 for a correct expression for $a$ (allow use of the letter $b$ )		
	$2^{\text{nd}}$ M1 for a correct expression for $a$ (allow use of the letter $b$ ) A1 for $y = 0.746 + 0.102x$ ( $a = \text{awrt } 0.746$ and $b = \text{awrt } 0.102$ ) Must be in $y$		
	and x and no fractions.	•	
(c)	100000		
	1 <sup>st</sup> A1 c = awrt 23600-23800		
Alt	$2^{\text{nd}} \text{ A1 } d = 1020^{**}$ answer given so must come from co Using $S_{sv} = 1000000S_{xy}$ and $S_{ss} = 100S_{xx}$ to find $d$ and using $S_{sv} = 100S_{xy}$ and $S_{ss} = 100S_{xx}$ to find $S_{sv} = 100S_{xy}$ to find $S_{sv} = 100S_{yy}$	_	
	$\overline{s} = 10\overline{x} + 50$ to find $c$ can score M1 provided fully corre	=	
( <b>d</b> )	M1 for substituting $s = 130$ into their (c) or substituting $x = 8$ into their (b)		
(a)	A1 awrt 156 000		
(e)	B1 A correct contextualised interpretation of the numer gradient which must mention $m^2$ or floor size and £ or $m^2$		
	through from their regression equation in (c)	- · · · · - <del> · ·</del> ·	
<b>(f)</b>	B1 awrt (£)32 000		

Question	Scheme	Marks	
3(a)	$[P(Female) =] \frac{30}{90} \text{ oe}$	B1	
	90	(1)	
(b)	$[P(Male   < 4 \text{ years}) =] \frac{P(Male \cap < 4 \text{ years})}{P(< 4 \text{ years})} = \frac{\frac{16}{(90)}}{\frac{16+9}{(90)}} = \frac{16}{25} \text{ oe}$	M1A1	
	$P(< 4 \text{ years})$ $\frac{16+9}{(90)}$ 25		
(c)	$P(Male \cap < 10 \text{ years}) = \frac{20+16}{(00)} = 36$	(2)	
	$[P(Male \mid < 10 \text{ years}) =] \frac{P(Male \cap < 10 \text{ years})}{P(< 10 \text{ years})} = \frac{\frac{20+16}{(90)}}{\frac{9+16+14+20}{(90)}} = \frac{36}{59}$	M1A1	
(1)	16	(2)	
(d)	$P(Male   < 4 \text{ years}) = \frac{16}{25}, P(Male) = \frac{60}{90}$ or		
	$P(< 4 \text{ years}   \text{Male}) = \frac{16}{60},  P(< 4 \text{ years}) = \frac{25}{90}  \underline{\text{or}}$	M1	
	P(Male $\cap$ < 4 years) = $\frac{16}{90}$ , P(Male) = $\frac{60}{90}$ , P(< 4 years) = $\frac{25}{90}$		
	$P(M \mid <4) \neq P(M) \text{ or } P(<4 \mid M) \neq P(<4) \text{ or}$ $P(Male \cap <4 \text{ years}) \neq P(M) \times P(<4)$	M1	
	so not independent.	A1	
		(3) <b>Total 8</b>	
	Notes		
(a)	B1 for $\frac{30}{90}$ or exact equivalent		
(b)	M1 for a correct ratio expression with at least one correct probability substituted or for a correct ratio of probabilities. num>denom is M0		
	A1 $\frac{16}{25}$ or 0.64 (Correct answer scores 2 out of 2).		
(c)	M1 for a correct ratio expression with at least one correct probability substituted or for a correct ratio of probabilities. num>denom is M0.		
	A1 $\frac{36}{59}$ or condone awrt 0.610 (must be 3sf) (Correct answer gets 2 out of 2).		
(d)	1 <sup>st</sup> M1 for stating all of the required numerical probabilities for a correct test which must be labelled. The probabilities must be correct or correct ft from (b)		
	(If attempting the first test, P(Male   < 4 years) = $\frac{16}{25}$ was found in part(b) and		
	need not be fully restated here).		
	2 <sup>nd</sup> M1 for <u>use</u> of a correct test. Must see the product if attempting the 3 <sup>rd</sup> test. A1 for correct test with all probabilities correct <u>and</u> a correct conclusion.		
	NB Use of A and B throughout scores M0M0A0 unless A and B are explicitly defined.		

Question	Scheme	Marks
4.(a)	[P(both blue) = $\frac{1}{20} \times \frac{1}{20} = ]\frac{1}{400}$ oe	B1
(b)	P(exactly 1 red) = $2 \times \frac{1}{20} \times \frac{19}{20}$ , = $\frac{19}{200}$ oe	(1) M1, A1
(c)	P(2 yellow and 1 green)= $3 \times \frac{4}{9} \times \frac{5}{8} \times \frac{4}{7} = \frac{10}{21}$ oe	(2) B1 M1 A1
(d)	P(All beads are yellow) = $\frac{5}{9} \times \frac{4}{8} \times \frac{3}{7} \times \frac{2}{6}$	M1 (3)
	P(At least 1 bead is green) = 1 - P(All beads are yellow)	
	$1 - \frac{5}{9} \times \frac{4}{8} \times \frac{3}{7} \times \frac{2}{6} = \frac{121}{126}$	M1A1
		(3) <b>Total 9</b>
	Notes	10(a) 9
(a)	B1 $\frac{1}{400}$ or 0.0025	
(b)	M1 for a correct equivalent expression $\frac{1}{20} \times \frac{19}{20} + \frac{19}{20} \times \frac{1}{20}$	
	A1 $\frac{19}{200}$ or 0.095	
(c)	B1 for $3 \times$ or for the sum of exactly 3 identical products attempted M1 for any one product correct	
	A1 $\frac{10}{21}$ (allow awrt 0.476 from correct working)	
( <b>d</b> )	$1^{\text{st}} \text{ M1 } \frac{5}{9} \times \frac{4}{8} \times \frac{3}{7} \times \frac{2}{6}$	
	$2^{\text{nd}}$ M1 Use of $1-n$ (where n is a product of 4 probabilities)	
	A1 $\frac{121}{126}$ (condone awrt 0.960 must be at least 3sf from correct working)	
	OR 1 <sup>st</sup> M1 List <b>all</b> 15 favourable outcomes <u>and</u> at least one correct product (YYYG)×4 [(YYGY), (YGYY), (GYYY)]	
	(YYGG)×6 [(YGYG), (YGGY), (GYYG), (GYGY), (GGYY)] (GGYG)×4 [(GGGY), (YGGG), (GYGG)] (GGGG)	
	2 <sup>nd</sup> M1 Sum all 15 correct probabilities	
	A1 $\frac{121}{126}$ (condone awrt 0.960 must be at least 3sf from correct working)	

Question	Scheme	Marks	
5.(a)	, , , , , , , , , , , , , , , , , , ,	B1 dB1	
(b)	$P(X > 70) = P\left(Z > \frac{70 - 55}{20}\right)$ $= P(Z > 0.75)$ $= 1 - 0.7734 = 0.2266$ awrt <u>0.227/22.7%</u>	(2) M1 M1A1	
(c)	$P(X > b) = 0.01$ $\frac{b - 55}{20} = 2.3263$	(3) M1B1	
( <b>d</b> )	$b = 101.526$ $P(70 < X < m) = 0.1315$ $P(X < m) - P(X < 70) = 0.1315$ $P\left(Z < \frac{m - 55}{20}\right) = 0.9049$	A1 (3) M1	
	$\frac{m-55}{20} = 1.31$ $m = 81.2$	M1B1 A1 (4) Total 12	
(a)	Notes  1 <sup>st</sup> B1 for a reasonable sketch of a symmetric, bell shaped curve which does not cross the <i>x</i> -axis (ignore any vertical axis drawn)  2 <sup>nd</sup> B1 dependent on previous B1 for 55 labelled at the centre of the <i>x</i> -axis		
<b>(b)</b>	$2^{\text{nd}}$ M1 Use of $1-p$ (must be a probability so $1-0.67$ is M0)		
(c)	A1 awrt 0.227 or 22.7% M1 for standardising with 55, 20 and equating to z-value $ z >2$ B1 for 2.3263 (or better) used and compatible sign with their standardisation. A1 for awrt 102 which must come from a z-value in the range $2.32 \le z \le 2.34$		
(d)	$1^{\text{st}}$ M1 for a correct expression for $P(X < m)$ (e.g. $0.1315 + `0.7734`$ ) or $P(X > m) = 0.0951$ or sight of 0.9049 (may be implied by sight of 1.31) $2^{\text{nd}}$ M1 for standardising with 55, 20 and equating to a z-value $ z  > 1$ B1 1.31 (1.31018from calc) used and compatible sign with their standardisation A1 awrt 81.2	on.	

Question	Scheme	Marks
6(a)	$F(3) = \frac{3}{4}$	B1
	4	(1)
(b)	E(X) = 2.5	B1
(c)	1 1 1 1 157	(1)
	$E(X^{2}) = 1^{2} \times \frac{1}{4} + 2^{2} \times \frac{1}{4} + 3^{2} \times \frac{1}{4} + 4^{2} \times \frac{1}{4} \left[ = \frac{15}{2} \right]$	M1
	$Var(X) = \frac{15}{2} - \left(\frac{5}{2}\right)^2 = \frac{5}{4} * *$	M1A1 cso (3)
(d)	$P(Y=y) = \frac{1}{4}$	B1
(e)	Var(Y) = Var(kX + c) =	(1)
	$k^2 \operatorname{Var}(X)$	M1
	$=\frac{5}{4}k^2$	A1
	7	(2)
( <b>f</b> )	c = 3 - k	B1 (1)
		(1) <b>Total 9</b>
	Notes	
(a)	B1 $\frac{3}{4}$ oe	
(b)	B1 2.5 oe	
(c)	1 <sup>st</sup> M1 for correct expression for E( $X^2$ ). $\frac{15}{2}$ on its own does not imply this mark	
	$2^{\text{nd}}$ M1 for correct expression for Var(X) (follow through their E(X <sup>2</sup> ) and E(X))	
	A1 for $\frac{5}{4}$ cso	
Alt (c)	1 <sup>st</sup> M1 for writing or using $Var(X) = \frac{n^2 - 1}{12}$ (may be implied by 2 <sup>nd</sup> M1)	
	$2^{\text{nd}}$ M1 for $\frac{4^2 - 1}{12}$ or $\frac{(4+1)(4-1)}{12}$ (15/12 on its own does not score this mark)	
	A1 $\frac{5}{4}$ cso (dependent on both M marks and no incorrect working seen)	
(d)	B1 $\frac{1}{4}$ may be in a table, but must be $\frac{1}{4}$ for each probability.	
(e)	M1 for $k^2 Var(X)$	
	A1 oe	
	Note: $Var(Y) = \frac{3^2 + (3+k)^2 + (3+2k)^2 + (3+3k)^2}{4} - \left(\frac{(3+(3+3k))^2}{2}\right)^2$ oe scores	M1A1 (if
	the correct expression is seen, we can isw)	

7.(a)  P A 80 -	
70 - *	
60 –	
50 —	
40 —	B1B1 (- 1ee)
30	
20 <b>X X X</b>	
10	
O 10 20 30 40 50 b	(2)
(b) For any sensible comment about H being far away from the other points. e.g. 'H is an outlier/anomaly', 'The blood protein/p/70 for H is much higher than the other patients', 'H does not follow the (linear) pattern', 'Data collected for H may be incorrect', etc.	B1
(c) $r = \frac{369}{\sqrt{423\frac{5}{7} \times 490}} = 0.809826106$	(1) M1A1
(d) $r$ would be closer to 0	B1 (2)
	Total 6
Notes (a) USING OVERLAY B1B1 all 8 points correctly plotted ½ small square	
(a) USING OVERLAY B1B1 all 8 points correctly plotted ½ small square tolerance. 7 points correct B1B0	
(b) Do not allow 'H is not in range' on its own	
(c) M1 for a correct expression A1 awrt 0.810 (Accept 0.81 if a fully correct expression is seen)	
(d) B1 allow $r$ would be smaller/weaker correlation	

Question	Scheme		Marks
8.(a)	(Time is) <u>continuous</u>		B1
(b)	40 people = 8 large squares/200 small squares 200 people = 40 large squares/1000 small squares 40/(21 – 11) or correct scale on f.d. axis		
	$\frac{x}{40} = \frac{180}{200}$ or $\frac{x}{40} = \frac{7.2}{8}$ or $(21-18) \times 4 + (25-21) \times 6$		
	36 people (spent between 18 and 25 min	nutes shopping in the supermarket)	A1 (3)
(c)	Median = $26 + \frac{[30]}{36} \times 5 = \text{awrt } \underline{30.2}$		M1A1 (2)
(d)	$\sum fx = 16 \times 40 + 23.5 \times 30 + 28.5 \times 36 + 33.5 \times 40 + 38.5 \times 14 + 46 \times 20 + 61 \times 20$ $= 6390 **$		
(e)	$i \ \overline{x} = \frac{6390}{200} = 31.95$		
( <b>f</b> )	ii $\sigma = \sqrt{\frac{238430}{200} - 31.95^2} = \sqrt{171.3475} = 13.09 \text{ (or } s = 13.122)$ awrt <u>13.1</u> 0.409 awrt <u>0.4</u>		M1A1 (3) B1 (1)
(g)	Method 1	Method 2 (see note)	
	(positive) skew or median ≠ mean oe	(almost) symmetric oe	B1
	not a good decision	a good decision	dB1
(a)	No		
(a) (b)	Allow not discrete. Condone misspellings if intention of 'continuous' is clear. B1 for establishing a ratio (usually 5 or 1/5) between people and area or calculating f.d. (may be implied by M1) M1 for a correct ratio or expression using areas for the people from 18 to 25 A1 36 cao (Answer of 36 scores 3 out of 3).		
(c)	M1 for an attempt at the medians (should have 26, 36 and 5). If working down $31 - \frac{[6]}{36} \times 5$		
(d)	A1 awrt 30.2 (can come from using $(n+1)$ ) M1 for a correct expression for $\sum fx$ condone one incorrect product A1cso for 6390 and all correct		
(e)( i) (ii) (g)	B1 31.95 or equivalent fraction M1 for correct expression for standard deviation including root A1 awrt 13.1 (answer of awrt 13.1 scores 2 out of 2) [NB ( $s = 13.122$ )]  1st B1 for comment on skew (may be seen in part (f)). Method 1: skew or median $\neq$ mean Only allow method 2 if  their(f)  < 0.45. Method 2: ~symmetric (any mention of correlation is B0)  2nd dB1 for a correct compatible comment about the manager's decision		

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